

Starter

Factorise fully:

- 1)  $4a^2b - 6abc$
- 2)  $3x^2 + 18x + 24$
- 3)  $2x^2 - 18$
- 4)  $2x^2 - x - 6$

30 seconds to write down EVERY square number between 1 and 100

4 16 64  
 9 25  
 49 36 81  
 100 1



A surd is a square root which doesn't 'work out' as a rational number.

eg.  $\sqrt{5}$  and  $\sqrt{3}$  are surds  
 $\sqrt{4}$  isn't, because  $\sqrt{4} = 2$   
 $2^2 = 4$   
 $\sqrt{4} = 2$

Today's Learning:

To simplify surds.

Rules of Surds

22/8/17

A surd is a root that doesn't work out nicely - they are irrational numbers.

1)  $\sqrt{m} \times \sqrt{n} = \sqrt{mn}$

2)  $\frac{\sqrt{m}}{\sqrt{n}} = \sqrt{\frac{m}{n}}$

e.g. Simplify:

1)  $\sqrt{12}$   
 $= \sqrt{4 \times 3}$   
 $= \sqrt{4} \times \sqrt{3}$   
 $= 2 \times \sqrt{3} = 2\sqrt{3}$

2)  $\sqrt{5} \times \sqrt{10}$   
 $= \sqrt{50}$   
 $= \sqrt{25 \times 2}$   
 $= \sqrt{25} \times \sqrt{2}$   
 $= 5 \times \sqrt{2} = 5\sqrt{2}$

3)  $5\sqrt{2} \times 3\sqrt{6}$   
 $= 15\sqrt{12}$   
 $= 15\sqrt{4 \times 3}$   
 $= 15 \times \sqrt{4} \times \sqrt{3}$   
 $= 15 \times 2 \times \sqrt{3}$   
 $= 30\sqrt{3}$

4)  $\sqrt[3]{\frac{3}{27}}$   
 $= \sqrt[3]{\frac{3}{27}}$   
 $= \sqrt[3]{\frac{1}{9}}$   
 $= \sqrt[3]{\frac{1}{9}}$   
 $= \frac{1}{3}$

Starter

Fully factorise the following:

1)  $x^2 + 7x + 10$

$(x+5)(x+2)$   
 10, 1

3)  $x^2 - 4$

$(x-2)(x+2)$

2)  $2x^2 - 16x + 14$

$2(x^2 - 8x + 7)$   
 $2(x-1)(x-7)$

4)  $2x^2 + 13x + 15$

$(2x+3)(x+5)$

Challenge:

Simplify

$$\begin{aligned} & \sqrt{12} + \sqrt{27} \\ &= \sqrt{4 \times 3} + \sqrt{9 \times 3} \\ &= 2\sqrt{3} + 3\sqrt{3} = 5\sqrt{3} \\ & \quad \quad \quad 2x + 3x \end{aligned}$$

Multiplying Out Brackets

e.g. Expand and simplify:

$$\begin{aligned} 1) & 2\sqrt{2}(3-\sqrt{2}) & 2\sqrt{2} \times \sqrt{2} \\ &= 6\sqrt{2} - 2\sqrt{4} & 2\sqrt{2} \times 2 \\ &= 6\sqrt{2} - 2 \times 2 & = 2\sqrt{4} \\ &= 6\sqrt{2} - 4 & \\ \\ 2) & (6-\sqrt{2})^2 & \\ &= (6-\sqrt{2})(6-\sqrt{2}) & \\ &= 36 - 6\sqrt{2} - 6\sqrt{2} + \sqrt{4} & \\ &= 36 - 12\sqrt{2} + 2 & \\ &= 38 - 12\sqrt{2} & \\ \\ 3) & (3+\sqrt{2})(4-2\sqrt{2}) & 3 \times 2x = 6x \\ &= 12 - 2\sqrt{4} - 6\sqrt{2} + 4\sqrt{2} & \\ &= 12 - 2 \times 2 - 2\sqrt{2} & \\ &= 8 - 2\sqrt{2} & \end{aligned}$$

Rationalising the Denominator

We don't like to have surds on the bottom of fractions, so we rationalise the denominator.

$$\begin{aligned} \text{e.g. 1) } & \frac{\sqrt{6}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{18}}{\sqrt{9}} = \frac{\sqrt{9 \times 2}}{3} \\ & = \frac{3\sqrt{2}}{3} = \sqrt{2} \\ \\ 2) & \frac{7}{\sqrt{8}} \times \frac{\sqrt{8}}{\sqrt{8}} = \frac{7\sqrt{8}}{\sqrt{64}} = \frac{7\sqrt{4 \times 2}}{8} \\ & = \frac{7 \times 2 \times \sqrt{2}}{8} \\ & = \frac{14\sqrt{2}}{8} = \frac{7\sqrt{2}}{4} \end{aligned}$$

Adding/Subtracting SurdsTreat the surd like an  $x$  in algebra.

$$\begin{aligned} \text{e.g. 1) Simplify } & \sqrt{18} - \sqrt{8} \\ &= \sqrt{9 \times 2} - \sqrt{4 \times 2} \\ &= 3\sqrt{2} - 2\sqrt{2} \\ &= \sqrt{2} \end{aligned}$$

$$\begin{aligned} 2) \text{ Simplify } & \sqrt{45} + \sqrt{5} - \sqrt{20} \\ &= \sqrt{9 \times 5} + \sqrt{5} - \sqrt{4 \times 5} \\ &= 3\sqrt{5} + \sqrt{5} - 2\sqrt{5} \\ &= 2\sqrt{5} \end{aligned}$$

Today's Learning

To rationalise the denominator of any surd by using a conjugate surd.

$$\begin{aligned} \frac{3}{\sqrt{20}} \times \frac{\sqrt{20}}{\sqrt{20}} &= \frac{3\sqrt{20}}{\sqrt{400}} \\ &= \frac{3\sqrt{4 \times 5}}{\sqrt{4 \times 100}} \\ &= \frac{3 \times 2 \times \sqrt{5}}{2 \times 10} \\ &= \frac{6\sqrt{5}}{20} = \frac{3\sqrt{5}}{10} \end{aligned}$$

$$\frac{4\sqrt{5}}{5\sqrt{3}} \times \frac{5\sqrt{3}}{5\sqrt{3}} = \frac{20\sqrt{15}}{25\sqrt{9}}$$

$$= \frac{20\sqrt{15}}{25 \times 3} = \frac{20\sqrt{15}}{75} = \frac{4\sqrt{15}}{15}$$

$$\frac{4\sqrt{5} \times 5\sqrt{3}}{4 \times 5 \times 5 \times \sqrt{3}}$$

Multiply out the brackets and simplify:

a)  $(2 + \sqrt{3})(2 - \sqrt{3}) = 4 - 2\sqrt{3} + 2\sqrt{3} - \sqrt{9} = 4 - 3 = 1$

b)  $(2\sqrt{3} + \sqrt{2})(2\sqrt{3} - \sqrt{2}) = 4\sqrt{9} - 2\sqrt{6} + 2\sqrt{6} - \sqrt{4} = 4 \times 3 - 2 = 12 - 2 = 10$

**Rationalising the Denominator**

When there is more than one term on the bottom of the fraction, use the **conjugate surd** (the same terms with the opposite sign).

e.g. 1)  $\frac{10}{7 + \sqrt{5}} \times \frac{(7 - \sqrt{5})}{(7 - \sqrt{5})} = \frac{70 - 10\sqrt{5}}{49 - 7\sqrt{5} + 7\sqrt{5} - 5}$

$$= \frac{70 - 10\sqrt{5}}{49 - 5}$$

$$= \frac{70 - 10\sqrt{5}}{44}$$

$$= \frac{35 - 5\sqrt{5}}{22}$$

2)  $\frac{2}{\sqrt{3} - \sqrt{2}} \times \frac{(\sqrt{3} + \sqrt{2})}{(\sqrt{3} + \sqrt{2})} = \frac{2\sqrt{3} + 2\sqrt{2}}{\sqrt{9} + \sqrt{6} - \sqrt{6} - \sqrt{4}}$

$$= \frac{2\sqrt{3} + 2\sqrt{2}}{3 - 2}$$

$$= \frac{2\sqrt{3} + 2\sqrt{2}}{1}$$

$$= 2\sqrt{3} + 2\sqrt{2}$$

~~$\frac{\sqrt{2}+1}{\sqrt{2}+1}$~~   
page 5  
Q14

**Exit Question:**

Rationalise the denominator:

$$\frac{3}{\sqrt{2} - 4}$$

**Starter**

Rationalise the denominators and simplify where possible:

1)  $\frac{2}{\sqrt{3}}$  2)  $\frac{1}{3\sqrt{6}}$  3)  $\frac{5}{4 - \sqrt{2}}$

$$\frac{2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

$$\frac{1}{3\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \frac{\sqrt{6}}{3\sqrt{36}} = \frac{\sqrt{6}}{18}$$

$$\frac{5}{4 - \sqrt{2}} \times \frac{(4 + \sqrt{2})}{(4 + \sqrt{2})} = \frac{5(4 + \sqrt{2})}{16 - 2} = \frac{20 + 5\sqrt{2}}{14}$$

4)  $\frac{3}{\sqrt{2} - \sqrt{8}}$

$$\frac{3}{\sqrt{2} - \sqrt{8}} \times \frac{(\sqrt{2} + \sqrt{8})}{(\sqrt{2} + \sqrt{8})} = \frac{3\sqrt{2} + 3\sqrt{16}}{\sqrt{4} + \sqrt{16} - \sqrt{16} - \sqrt{64}}$$

$$= \frac{3\sqrt{2} + 3 \times 2}{2 - 8} = \frac{3\sqrt{2} + 6}{-6}$$

$$= \frac{3\sqrt{2} + 6\sqrt{2}}{-6} = \frac{9\sqrt{2}}{-6}$$

**Today's Learning:**

To multiply and divide indices and to raise indices to powers.

$$m^5$$

$$m \times m \times m \times m \times m$$

Rules of Indices

5 is the index in  $a^5$ . This means  $a \times a \times a \times a \times a$

Rules:

- 1)  $a^m \times a^n = a^{m+n}$
- 2)  $\frac{a^m}{a^n} = a^{m-n}$
- 3)  $(a^m)^n = a^{mn}$

e.g. Simplify:

1)  $\frac{g^3 \times g^2}{g^4} = \frac{g^5}{g^4} = g^1 = g$

2)  $(2h^3)^2 = 4h^6$

3)  $r^2(r+r^5) = r^3 + r^7$

What is  $2^2 \times 2^3$ ?

$$2 \times 2 \times 2 \times 2 \times 2 = 2^5$$

What is  $2^5 \div 2^2$ ?

$$\frac{2 \times 2 \times 2 \times 2 \times 2}{2 \times 2} = 2^3$$

What is  $(2^3)^2$ ?

$$2 \times 2 \times 2 \times 2 \times 2 \times 2 = 2^6$$

Starter

1) Find the gradient of the straight line that joins (-2, -3) to (-4, -1).

$$gr = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - (-3)}{-4 - (-2)} = \frac{2}{-2} = -1$$

2) The area of a semicircle is  $14\text{cm}^2$ . Find its radius.

$$28 = \pi r^2$$

$$\frac{28}{\pi} = r^2$$

$$r = 2.99$$

3) If all the numbers from 1 to 20 are on cards, and I pick one at random, what is the probability it is a prime number?

2, 3, 5, 7, 11, 13, 17, 19

$$\frac{8}{20} = \frac{2}{5}$$

387.04

4) Calculate 82% of 472.

Today's Learning:

To simplify indices with negative and fractional powers.

Rules of Indices

- 5)  $a^{-m} = \frac{1}{a^m}$
- 6)  $a^{\frac{m}{n}} = \sqrt[n]{a^m}$

e.g. rewrite with a positive index:

1)  $4^{-4} = \frac{1}{4^4}$

2)  $2b^{-3} = 2 \times \frac{1}{b^3} = \frac{2}{b^3}$

3)  $\frac{3}{y^{-5}} = 3y^5$

2) find the value of

a)  $27^{\frac{2}{3}} = \sqrt[3]{27^2} = 3^2 = 9$

b)  $1000^{-\frac{2}{3}} = \frac{1}{1000^{\frac{2}{3}}} = \frac{1}{\sqrt[3]{1000^2}} = \frac{1}{10^2} = \frac{1}{100}$

Today's Learning:

Multiplying out brackets using indices and trying exam type questions.

Multiplying out Brackets

e.g. 1)  $\sqrt{x}(x^2 - 1) = x^{\frac{1}{2}}(x^2 - 1)$   
 $= x^{2.5} - x^{1/2}$

2)  $\left(x + \frac{1}{x^2}\right)^2 = (x^1 + x^{-2})(x^1 + x^{-2})$   
 $= x^2 + x^{-1} + x^{-1} + x^{-4}$   
 $= x^2 + 2x^{-1} + x^{-4}$

3)  $\frac{x+2}{x^2}$

Today's Learning:

To use indices in scientific notation.

Standard Form

A number is expressed as  $m \times 10^n$ , where  $1 \leq m < 10$ .

Examples. Write your answer in standard form:

1) A space probe can travel at a speed of  $3.6 \times 10^6$  miles per day. What distance can it travel in a week?

$$\begin{array}{r} 3.6 \\ 4 \times 7 \\ \hline 25.2 \end{array}$$

$$7 \times 3.6 \times 10^6 = 25.2 \times 10^6 = 2.52 \times 10 \times 10^6 = 2.52 \times 10^7$$

2)  $(2 \times 10^{-8}) \times (3.5 \times 10^2)$

$$= 2 \times 3.5 \times 10^{-8} \times 10^2 = 7 \times 10^{-6}$$

Starter

Factorise fully:

1)  $6x^2 - 4x$

$2x(3x - 2)$

3)  $9m^2 - 25$

$(3m + 5)(3m - 5)$

2)  $x^2 + 5x - 14$

$(x + 7)(x - 2)$

4)  $2x^2 - 5x - 3$

$(2x + 1)(x - 3)$

Rewrite these numbers in full:

a) The speed of light:  $3 \times 10^8$  m/s

300000000

b) The diameter of the earth:  $1.268 \times 10^4$  km

12680

c) The approximate population of the earth:  $7.4 \times 10^9$

7400000000

d) The number of dollars Bill Gates is worth:  $7.92 \times 10^{10}$

79200000000

e) The radius of the orbit of an electron:  $5 \times 10^{-8}$

0.00000005

Starter

2) Rationalise the denominator:

1) Simplify  $\sqrt{75} - \sqrt{12}$

$$\begin{aligned} &= \sqrt{25 \times 3} - \sqrt{4 \times 3} \\ &= 5\sqrt{3} - 2\sqrt{3} \\ &= 3\sqrt{3} \end{aligned}$$

$$\frac{3}{2\sqrt{6}} = \frac{3}{2\sqrt{6}} \times \frac{\sqrt{6}}{\sqrt{6}} = \frac{3\sqrt{6}}{2 \times 6} = \frac{3\sqrt{6}}{12} = \frac{\sqrt{6}}{4}$$

$$\begin{aligned} p^2 \div p &= p \\ p \times p &= p^2 \end{aligned}$$

$$\begin{aligned} p^2 \div p^2 &= 1 \\ p^2 \times 1 &= p^2 \end{aligned}$$

3) Simplify:

a)  $(p^3)^4 \times p^{-4}$

$$\begin{aligned} &= p^{12} \times p^{-4} \\ &= p^8 \end{aligned}$$

b)  $\frac{p^3 \times p^{-1}}{p^2}$

$$\begin{aligned} &= \frac{p^2}{p^2} \\ &= p^0 = 1 \end{aligned}$$

c)  $\frac{7}{h^2} \div h$

$$\begin{aligned} &= 7h^{-2} \div h^1 \\ &= 7h^{-3} \end{aligned}$$

d)  $p^{\frac{2}{3}} \times \sqrt[3]{p}$

$$\begin{aligned} &= p^{\frac{2}{3}} \times p^{\frac{1}{3}} \\ &= p^1 = p \end{aligned}$$

Today's Learning:

To revise surds and indices work.

Simplify  $2\sqrt{27}$

$$\begin{aligned}
 &= 2\sqrt{9 \times 3} \\
 &= 2\sqrt{9} \times \sqrt{3} \\
 &= 2 \times 3 \times \sqrt{3} = 6\sqrt{3}
 \end{aligned}$$

Calculate  $2\sqrt{3} + \sqrt{12}$

$$\begin{aligned}
 &= 2\sqrt{3} + \sqrt{4 \times 3} \\
 &= 2\sqrt{3} + 2\sqrt{3} \\
 &= 4\sqrt{3}
 \end{aligned}$$

Rationalise the denominator:  $\frac{1}{2-\sqrt{3}}$

$$\begin{aligned}
 &\frac{1}{(2-\sqrt{3})} \times \frac{(2+\sqrt{3})}{(2+\sqrt{3})} \\
 &= \frac{2+\sqrt{3}}{4+2\sqrt{3}-2\sqrt{3}-9} \\
 &= \frac{2+\sqrt{3}}{4-3} \\
 &= \frac{2+\sqrt{3}}{1} = 2+\sqrt{3}
 \end{aligned}$$