

Starter

1) Solve for T:

$5T < 8T - 3$

$5T + 3 < 8T$   
 $3 < 3T$   
 $1 < T$

2) Simplify:

$\frac{3m^2 - 6m}{m^2 - 8m + 12}$

$= \frac{3m(m-2)}{(m-6)(m-2)}$   
 $x^2 \times x^3 = x^5 = \frac{3m}{m-6}$

3) Simplify:

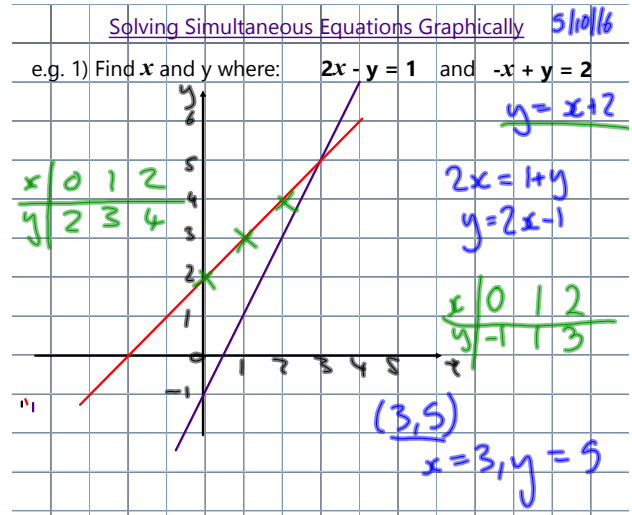
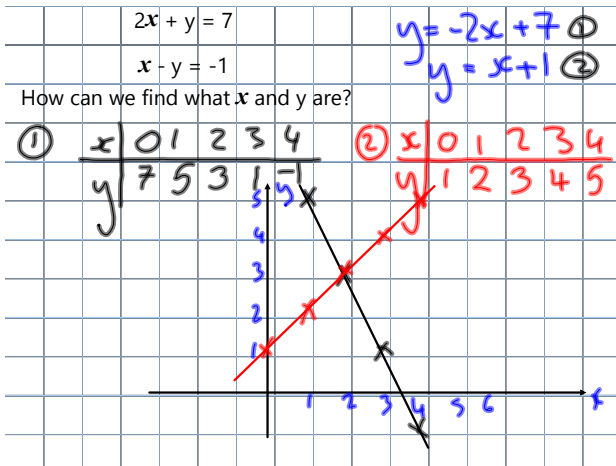
$\frac{C}{\sqrt[3]{C^2}} = \frac{C^1}{C^{2/3}} = C^{1/3} = \sqrt[3]{C}$

4) Solve for m:  $3(m - 2) = 2(3 - m) + 9$

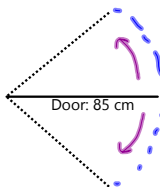
$3m - 6 = 6 - 2m + 9$   
 $5m - 6 = 15$   
 $5m = 21$   
 $m = 4\frac{1}{5}$

Today's Learning:

To solve simultaneous equations using graphs.



Starter



The door swings through an angle of 85°. Calculate the length of the dotted perimeter, so it can be marked out in tape.

Perimeter

Arc length =  $\frac{85}{360} \times \pi \times d$   
 $= \frac{85}{360} \times \pi \times 170$   
 $= 126.1 \text{ cm.}$

Perimeter =  $85 + 85 + 126.1 \text{ cm}$   
 $= 296 \text{ cm}$

Today's Learning:

Solving simultaneous equations using substitution.

In McDonalds, Georgia bought 2 happy meals, and paid 8€. Harry got a happy meal and a McFlurry and paid 6€.  
How much does each item cost?

$$\begin{aligned} 2h &= 8 && \rightarrow h=4 \\ h + m &= 6 \\ 4 + m &= 6 \\ m &= 2 \end{aligned}$$

Mike wanted to know the price of tickets and popcorn at the cinema.

All he knows is that James bought 2 tickets and 1 popcorn and that cost £28, and Sarah bought 1 ticket and 3 popcorns and that cost £24.

How could he figure out the price of popcorn and of tickets?

$$\begin{aligned} 2T + P &= 28 \text{ (1)} && T + 3P = 24 \text{ (2)} \\ T &= 24 - 3P && \times 2 \quad \times 2 \\ 2(24 - 3P) + P &= 28 && 2T + 6P = 48 \text{ (3)} \\ 48 - 6P + P &= 28 && \\ 20 - 5P &= 0 && \\ 20 &= 5P && \\ P &= 4 && \\ 5P &= 20 && \\ P &= 4 && \\ 2T + 4 &= 28 && \\ 2T &= 24 && \\ T &= 12 && \end{aligned}$$

5/10/16 Simultaneous Equations - Substitution

e.g. Find x and y if  $3x + 2y = 18$  and  $y - x = -1$

$$\begin{aligned} y &= x - 1 \\ 3x + 2(x - 1) &= 18 \\ 3x + 2x - 2 &= 18 \\ 5x - 2 &= 18 \\ 5x &= 20 \\ x &= 4 \\ 3x + 2y &= 18 \\ 12 + 2y &= 18 \\ 2y &= 6 \\ y &= 3 \end{aligned}$$

Solving by elimination:

$$\begin{aligned} 2y + x &= 5 \\ 4y - x &= 7 \\ \hline 6y &= 12 \\ y &= 2 \\ x &= 1 \end{aligned}$$

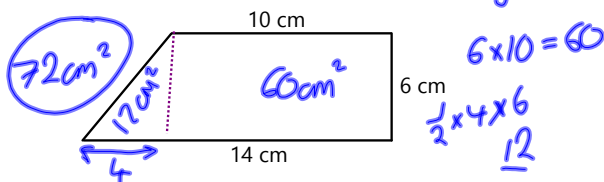
Starter

1) Fully factorise:  $2m^3 + 14m^2 + 24m$   
 $= 2m(m^2 + 7m + 12)$   
 $= 2m(m + 3)(m + 4)$

2) Solve for g:  $2g + 9 > -g$

$$\begin{aligned} 2g & & -2g & \\ 9 & > & -3g & \\ \div 3 & & \div 3 & \\ 3 & > & -g & \rightarrow -3 < g \\ & & & g > -3 \end{aligned}$$

3) Find the area of the shape:



Today's Learning:

Solving Simultaneous Equations by elimination.

$T + B = 6$

$T - B = 4$

$$2T = 10$$

$$T = 5$$

$$5 - B = 4$$

$$B = 1$$

Solve the following pairs of simultaneous equations:

(a)  $x + y = 4$   
 $x - y = 2$

$$2x = 6$$

$$x = 3$$

$$y = 1$$

(b)  $x + y = 9$   
 $x - y = 5$

$$2x = 14$$

$$x = 7$$

$$y = 2$$

(c)  $x + y = 7$   
 $x - y = 3$

$$2x = 10$$

$$x = 5$$

$$y = 2$$

$$5 + y = 7$$

$$y = 2$$

$4b + 2c = 50$  ①

$2b + 2c = 30$  ②

$$\textcircled{2} \times (-1): -2b - 2c = -30$$

$$\textcircled{1}: 4b + 2c = 50$$

$$2b = 20$$

$$b = 10$$

$$4b + 2c = 50$$

$$40 + 2c = 50$$

$$2c = 10$$

$$c = 5$$

(d)  $3x + y = 9$  ①  
 $x + y = 5$  ②

$$\textcircled{2} \times (-1): -x - y = -5$$

$$\textcircled{1}: 3x + y = 9$$

$$2x = 4$$

$$x = 2$$

$$x + y = 5$$

$$2 + y = 5$$

$$y = 3$$

(e)  $4x + y = 11$  ①  
 $2x + y = 5$  ②

$$\textcircled{2} \times (-1): -2x - y = -5$$

$$\textcircled{1}: 4x + y = 11$$

$$2x = 6$$

$$x = 3$$

$$4x + y = 11$$

$$4(3) + y = 11$$

$$12 + y = 11$$

$$-12 \quad -12$$

$$y = -1$$

(f)  $7x + 2y = 36$  ①  
 $2x + 2y = 16$  ②

$$\textcircled{2} \times (-1): -2x - 2y = -16$$

$$\textcircled{1}: 7x + 2y = 36$$

$$5x = 20$$

$$x = 4$$

$$2x + 2y = 16$$

$$2(4) + 2y = 16$$

$$8 + 2y = 16$$

$$2y = 8$$

$$y = 4$$

$4b + c = 21$  ①

$2b + 3c = 13$  ②

$$\textcircled{1} \times (-3): -12b - 3c = -63$$

$$\textcircled{2}: 2b + 3c = 13$$

$$-10b = -50$$

$$b = 5$$

$$2b + 3c = 13$$

$$10 + 3c = 13$$

$$3c = 3$$

$$c = 1$$

**Starter**

1) At a cinema, Charlie bought 1 ticket and 1 packet of sweets and paid £10. At the same cinema, Sam bought one ticket and 2 packets of sweets and paid £12.

How much do tickets and packets of sweets cost?

$$T + S = 10$$
 ①  

$$T + 2S = 12$$
 ②  

$$-2 \times \textcircled{1}: -2T - 2S = -20$$
  

$$\textcircled{2}: T + 2S = 12$$
  

$$-T = -8$$
  

$$T = 8 \quad S = 2$$

2) 2 sandwiches and 3 teas cost £20. At the same restaurant, one sandwich and one tea cost £9.

How much does each item cost?

$$2s + 3T = 20$$
 ①  

$$s + T = 9$$
 ②  

$$-2 \times \textcircled{2}: -2s - 2T = -18$$
  

$$\textcircled{1}: 2s + 3T = 20$$
  

$$T = 2$$
  

$$s + 2 = 9$$
  

$$s = 7$$

$$2a + 3b = 40 \quad \textcircled{1}$$

$$3a + 2b = 35 \quad \textcircled{2}$$

$$\begin{aligned} 2 \times \textcircled{1}: & 4a + 6b = 80 \\ -3 \times \textcircled{2}: & -9a - 6b = -105 \\ \hline & -5a = -25 \\ & a = 5 \\ & 2a + 3b = 40 \\ & 10 + 3b = 40 \\ & 3b = 30 \\ & b = 10 \end{aligned}$$

### Solving Simultaneous Equations 7/10/16

- ★ Label the equations
- ★ Multiply each equation so you can cancel something out
- ★ Add the equations together
- ★ Solve
- ★ Substitute to find the other unknown

e.g. 1)  $7b - 5c = 35 \quad \textcircled{1}$

$$9b - 4c = 45 \quad \textcircled{2}$$

$$\begin{aligned} 4 \times \textcircled{1}: & 28b - 20c = 140 \\ -5 \times \textcircled{2}: & -45b + 20c = -225 \\ \hline & -17b = -85 \\ & b = 5 \\ & 7b - 5c = 35 \\ & 35 - 5c = 35 \\ & -5c = 0 \\ & c = 0 \end{aligned}$$

2)  $2x + 3y = 7 \quad \textcircled{1}$

$$4x + 5y = 12 \quad \textcircled{2}$$

$$\begin{aligned} -2 \times \textcircled{1}: & -4x - 6y = -14 \\ \textcircled{2}: & 4x + 5y = 12 \\ \hline & -y = -2 \\ & y = 2 \\ & 2x + 3y = 7 \\ & 2x + 6 = 7 \\ & 2x = 1 \\ & x = \frac{1}{2} \end{aligned}$$

### Starter

1) Simplify as much as possible:

a)  $\frac{2x^2 + 10x + 12}{2x + 6}$

$$\begin{aligned} &= \frac{2(x^2 + 5x + 6)}{2(x+3)} \\ &= \frac{2(x+5)(x+2)}{2(x+3)} \\ &= x+2 \end{aligned}$$

b)  $\sqrt[3]{c^4} \times \frac{1}{\sqrt[3]{c}}$

$$\begin{aligned} &= c^{\frac{4}{3}} \times c^{-\frac{1}{3}} \\ &= c^{\frac{4}{3} - \frac{1}{3}} \\ &= c^{\frac{3}{3}} \\ &= c \end{aligned}$$

c)  $\sqrt{40} - \sqrt{90}$

$$\begin{aligned} &= \sqrt{4 \times 10} - \sqrt{9 \times 10} \\ &= 2\sqrt{10} - 3\sqrt{10} \\ &= -\sqrt{10} \end{aligned}$$

Today's Learning:

Practising exam type questions.